

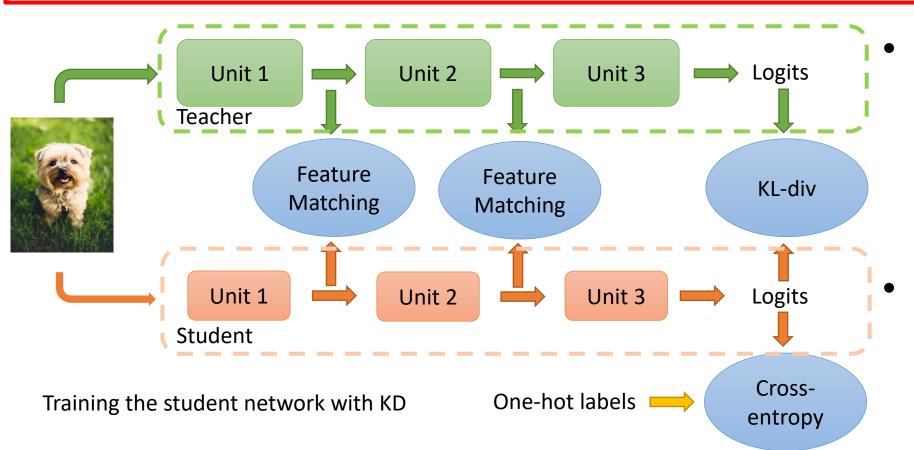
# Model Compression Using Optimal Transport

## **Suhas Lohit and Michael Jones**





## **Knowledge Distillation (KD)**



- Accurate deep neural networks for vision are usually very large and cannot be easily deployed in resourceconstrained settings
- Model compression is an important research direction to make networks smaller without losing accuracy
- KD is one of the main ways to achieve model compression, by transferring knowledge from a larger, more accurate teacher to a smaller student network.
- In order to train the student, the earliest methods used a combination of the usual cross-entropy loss with the K-L divergence b/w student and teacher outputs
- Student performance can be further improved using supervision at the intermediate layers by adding additional loss terms that encourage matching the teacher and student features. E.g., Fitnets and Relational KD

## Using optimal transport (OT) for feature matching

- Optimal transport matches student and teacher feature distributions in a principled way
- Unlike methods like FitNets, it relaxes the unnecessary requirement that teacher and student features need to match one-to-one
- It is a stronger condition than in Relational KD which only matches distance matrices computed in the teacher and student feature spaces

True class-boundary True class-boundary 
$$L_{OT}(X^{(l)},Y^{(l)}) = \min_{T \geq 0} \sum_{i,j} T_{i,j}^{(l)} C_{i,j}^{(l)}$$

teacher and student leature spaces 
$$\text{s.t.} \sum_{i} T_{i,j}^{(l)} = \sum_{i} T_{i,j}^{(l)} = \frac{1}{b},$$
 
$$L = L_{CE}(\mathbf{c}, \hat{\mathbf{c}}_S) + \alpha \sum_{i} L_{OT}(X^{(l)}, Y^{(l)}) + \gamma L_{KD}(\hat{\mathbf{c}}_S, \hat{\mathbf{c}}_T) \qquad C_{i,j}^{(l)} = 1 - \frac{\mathbf{x}_i^{(l)T} \mathbf{y}_j^{(l)}}{\|\mathbf{x}_i^{(l)}\| \|\mathbf{y}_i^{(l)}\|}$$

#### Relaxations of OT for KD

- We use relaxations of OT in order to solve the OT problems at multiple layers efficiently
- We experiment with
- Relaxed Earth Mover's Distance (REMD)
- **Inexact Proximal Optimal Transport**
- Both can be easily integrated with modern deep learning toolboxes

$$L_{ROT}(X^{(l)}, Y^{(l)}) = \min_{T \ge 0} \sum_{i,j} T_{i,j}^{(l)} C_{i,j}^{(l)} + \epsilon h(T)$$
s.t. 
$$\sum_{i,j} T_{i,j}^{(l)} = \sum_{i,j} T_{i,j}^{(l)} = \frac{1}{b},$$

$$R_{OT}^{(1)}(X^{(l)}, Y^{(l)}) = \min_{T \ge 0} \sum_{i,j} T_{i,j}^{(l)} C_{i,j}^{(l)} \quad \text{s.t.} \sum_{i} T_{i,j}^{(l)} = \frac{1}{b}$$

$$R_{OT}^{(2)}(X^{(l)}, Y^{(l)}) = \min_{T \ge 0} \sum_{i,j} T_{i,j}^{(l)} C_{i,j}^{(l)} \quad \text{s.t.} \sum_{i} T_{i,j}^{(l)} = \frac{1}{b}$$

$$R_{OT}^{(2)}(X^{(l)},Y^{(l)}) = \min_{T \geq 0} \sum_{i,j} T_{i,j}^{(l)} C_{i,j}^{(l)} \quad \text{s.t.} \sum_{j} T_{i,j}^{(l)} = \frac{1}{b}$$

The final relaxed EMD (REMD) is computed using

$$L_{REMD}(X^{(l)}, Y^{(l)})$$

$$= \max(R_{OT}^{(1)}(X^{(l)}, Y^{(l)}), R_{OT}^{(2)}(X^{(l)}, Y^{(l)}))$$

$$= \frac{1}{b} \max\left(\sum_{i} \min_{j} C_{i,j}^{(l)}, \sum_{j} \min_{i} C_{i,j}^{(l)}\right)$$

## Experimental results on image recognition datasets

#### **CIFAR-100**

Numbers shown are accuracies (higher is better)

Teacher Student	WRN-40-2 WRN-16-2	resnet110 resnet20	resnet32x4 resnet8x4	vgg13 vgg8	resnet32x4 ShuffleNetV2		
Teacher	75.61	74.31	79.42	74.64	79.42		
Student (no distillation)	73.26	69.06	72.50	70.36	71.82		
KD	74.92	70.67	73.33	72.98	74.45		
CRD+KD	75.64	71.56	75.46	74.29	76.05		
FitNet+KD	75.12	70.67	74.66	73.22	75.15		
RKD+KD	74.89	70.77	73.79	72.97	74.55		
REMD + KD	75.79	70.98	76.06	74.35	76.66		
IPOT + KD	75.63	71.29	75.99	74.29	<b>76.78</b>		
IPOT + CRD	75.57	71.47	76.06	74.30	76.81		
IPOT + CRD + KD	76.22	71.81	76.82	<b>74.79</b>	<b>76.81</b>		

#### **ImageNet**

Teacher: Resnet-34, Student: ResNet-18 Numbers shown are error rates (lower is better)

	Teacher	Student	KD	Online KD *	CRD	CRD+KD	AT	SP	CC	IPOT	IPOT+KD
				29.45							
Top-5	8.58	10.93	10.12	10.41	9.87	9.51	10.00	10.20	10.83	10.48	9.66

## **Street View House Numbers (SVHN)**

Numbers shown are accuracies (higher is better)

S pair	Teacher	Student	KD	CRD (	CRD+KD	FitNet F	itnet+KD	RKD R	KD+KD	PKT P	KT+KD	REMD RE	EMD+KD	IPOT IF	POT+KD
snet32x4 esnet8x4	94.36	90.39	94.49	94.96	95.47	91.32	94.48	93.30	94.58	90.77	94.38	89.66	94.49	91.63	94.73
RN-40-2 RN-16-2	94.52	93.45	95.22	94.74	95.25	93.93	95.27	95.23	95.39	93.68	95.15	93.15	94.94	94.28	95.41

#### Conclusion

- We have presented feature matching methods using optimal transport between teacher and student features at intermediate layers
- We have shown improved performance in knowledge distillation using optimal transport compared to methods like FitNets and RKD

#### References

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- 3. IPOT: Yujia Xie, Xiangfeng Wang, Ruijia Wang, and Hongyuan Zha. A fast proximal point method for computing exact Wasserstein distance, PMLR 2020
- 4. REMD: Matt Kusner, Yu Sun, Nicholas Kolkin, and Kilian Weinberger. From word embeddings to document distances, ICML 2015.